

# CS 61A

# DISCUSSION 7

## SCHEME

Raymond Chan  
Discussion 134  
UC Berkeley Fall 16

# AGENDA

- Announcements
- Scheme
  - Primitives
  - Call Expressions
  - Special Forms
  - Pairs and Lists

# ANNOUNCEMENTS

- Midterm 2
- Homework 9 extended to Monday 10/31
- Map composition revision Sunday 11/06

# SCHEME

- It's a "clean", functional programming language. (Dialect of Lisp)
  - <http://scheme.cs61a.org/>
- 4 main points:
  - **Everything is an expression.**
  - **All functions are hidden lambdas.**
  - **Everything is a symbol unless evaluated.**
  - **Non symbols are values (no objects).**

# PRIMITIVES

- Atomic primitive expressions cannot be divided up and evaluate to themselves.
- Numbers and booleans.
- The only false-y value in scheme is false (#f, False).
- Use nil instead of None.

# PRIMITIVES

- Atomic primitive expressions cannot be divided up and evaluate to themselves.
- Numbers and booleans.
- The only false-y value in scheme is false (#f, False).
- Use nil instead of None.

scm> 123

123

scm> 123.123

123.123

scm> #t

True

scm> #f

False

scm> nil

scm> ()

# VARIABLES & PROCEDURES

- **define** is a special form that defines **symbols** and **procedures** (functions).
- The equivalent of both assignment and def statements in Python. (no `a = 3` in Scheme)
- **Define** binds a value to a symbol.
- When a symbol / function is defined, returns the symbol.
  - In the function cause, the symbol is the procedure name.
  - The symbol has a value of a procedure.

# VARIABLES & PROCEDURES

- **(define <variable name> <value>)**
- **(define (<function name> <parameters>) <function body>)**
- <parameters> are split up by at least one space.

# VARIABLES & PROCEDURES

- **(define <variable name> <value>)**
- **(define (<function name> <parameters>) <function body>)**
- <parameters> are split up by at least one space.

```
scm> (define a 3)
```

```
a
```

```
scm> a
```

```
3
```

```
scm> (define (foo x) x)
```

```
foo
```

```
scm> (foo 5)
```

```
5
```

# VARIABLES & PROCEDURES

- **(define <variable name> <value>)**
- **(define (<function name> <parameters>) <function body>)**
- <parameters> are split up by at least one space.

```
scm> (define a 3)
```

```
a
```

```
scm> a
```

```
3
```

```
scm> (define (foo x) x)
```

```
foo
```

```
scm> (foo 5)
```

```
5
```

```
scm> (define (bar x y) (* x y))
```

```
bar
```

```
scm> (bar 4 5)
```

```
20
```

# SYMBOLS

- Any expression that is quoted is not evaluated. (Use single quote)
- They become symbols.
- Below, a is bound to the symbol of b

# WWSP

```
scm> (define a 1)
```

```
scm> a
```

```
scm> (define b a)
```

```
scm > b
```

```
scm> (define c 'a)
```

```
scm> c
```

# WWSP

```
scm> (define a 1)
```

```
a
```

```
scm> a
```

```
scm> (define b a)
```

```
scm > b
```

```
scm> (define c 'a)
```

```
scm> c
```

# WWSP

```
scm> (define a 1)
```

```
a
```

```
scm> a
```

```
1
```

```
scm> (define b a)
```

```
scm > b
```

```
scm> (define c 'a)
```

```
scm> c
```

# WWSP

```
scm> (define a 1)
```

```
a
```

```
scm> a
```

```
1
```

```
scm> (define b a)
```

```
b
```

```
scm > b
```

```
scm> (define c 'a)
```

```
scm> c
```

# WWSP

```
scm> (define a 1)
```

```
a
```

```
scm> a
```

```
1
```

```
scm> (define b a)
```

```
b
```

```
scm > b
```

```
1
```

```
scm> (define c 'a)
```

```
scm> c
```

When we define b, we eval a to be 1.  
Thus symbol b has value of 1.

# WWSP

```
scm> (define a 1)
```

```
a
```

```
scm> a
```

```
1
```

```
scm> (define b a)
```

```
b
```

```
scm > b
```

```
1
```

```
scm> (define c 'a)
```

```
c
```

```
scm> c
```

# WWSP

```
scm> (define a 1)
```

```
a
```

```
scm> a
```

```
1
```

```
scm> (define b a)
```

```
b
```

```
scm > b
```

```
1
```

```
scm> (define c 'a)
```

```
c
```

```
scm> c
```

```
a
```

Evaluate 'a as symbol a.  
c is has value symbol a.

# CALL EXPRESSIONS

- Use prefix notation.
- Call expressions starts off with an **operator** that is followed by zero or more **operand** subexpressions.
- Procedures (function) are called with parenthesis.
  - (**operator**) **operand1** **operand2** ...)
  - Open parenthesis "(" always starts a function call.
  - Spaces matter.

# CALL EXPRESSIONS

- ( <operand1> <operand2> ...)
- Operators can be symbols (+, \*, ...) or more complex expressions.
- Operators need to evaluate to procedure values.
- The first expression after "(" is the operator.
- Evaluate the operator and then each of the operands.
- Apply the operator to those evaluated operands.

# CALL EXPRESSIONS

```
scm> (- 1 1) ; 1 - 1
0
scm> (/ 8 4 2) ; 8 / 4 / 2
1
scm> (* (+ 1 2) (+ 1 2)) ; (1 + 2) * (1 + 2)
9
```

# CALL EXPRESSIONS

- Built-in functions:
  - +, -, \*, /
  - >, <, >=, <=
  - =      Checks for number equality
  - eq?    Checks equality for everything else
  - null?   Checks if the expression is nil

# WWSP

scm> (+ 1)

scm> (\* 3)

scm> (+ (\* 3 3) (\* 4 4))

scm> (define a (define b 3))

scm> a

scm> b

# WWSP

```
scm> (+ 1)
```

```
1
```

```
scm> (* 3)
```

Default start value for + is 0

```
scm> (+ (* 3 3) (* 4 4))
```

```
scm> (define a (define b 3))
```

```
scm> a
```

```
scm> b
```

# WWSP

```
scm> (+ 1)
```

```
1
```

```
scm> (* 3)
```

```
3
```

```
scm> (+ (* 3 3) (* 4 4))
```

Default start value for + is 1

```
scm> (define a (define b 3))
```

```
scm> a
```

```
scm> b
```

# WWSP

```
scm> (+ 1)
```

```
1
```

```
scm> (* 3)
```

```
3
```

```
scm> (+ (* 3 3) (* 4 4))
```

```
25
```

```
scm> (define a (define b 3))
```

```
scm> a
```

```
scm> b
```

# WWSP

```
scm> (+ 1)
```

```
1
```

```
scm> (* 3)
```

```
3
```

```
scm> (+ (* 3 3) (* 4 4))
```

```
25
```

```
scm> (define a (define b 3))
```

```
a
```

```
scm> a
```

```
scm> b
```

# WWSP

```
scm> (+ 1)  
1  
scm> (* 3)  
3  
scm> (+ (* 3 3) (* 4 4))  
25  
scm> (define a (define b 3))  
a  
scm> a  
b  
scm> b
```

(define b 3) returns symbol b  
a defined to have value symbol b

# WWSP

scm> (+ 1)

1

scm> (\* 3)

3

scm> (+ (\* 3 3) (\* 4 4))

25

scm> (define a (define b 3))

a

scm> a

b

scm> b

3

# SPECIAL FORMS

## IF STATEMENTS

- Expressions that look like function calls but don't follow the rules of evolution are called special forms (ex. `define`).
- `(if <condition> <then> <else>)`
  - Only #f is false-y. Everything else is truth-y.
  - To replicate Python's if, elif, else, we need to nest if expressions.

```
scm> (if (< 4 5) 1 2)  
1
```

```
scm> (if #f (/ 1 0) 42)  
42
```

# SPECIAL FORMS

## IF STATEMENTS

- Expressions that look like function calls but don't follow the rules of evaluation are called special forms (ex. `define`).
- `(if <condition> <then> <else>)`
  - Only #f is false-y. Everything else is truth-y.
  - To replicate Python's `if`, `elif`, `else`, we need to nest if expressions.

```
scm> (if #f (* 1 100)
        (if (= 4 5) 8 10))
```

# SPECIAL FORMS

## BOOLEAN OPERATORS

- **and, or, and not** work like the same in Python.
- **and** and **or** are special forms as they short-circuit.

```
scm> (and 1 2 3)
```

```
3
```

```
scm> (or 1 2 3)
```

```
1
```

```
scm> (or True (/ 1 0))
```

```
True
```

```
scm> (and False (/1 0))
```

```
False
```

```
scm> (not 3)
```

```
False
```

```
scm> (not True)
```

```
False
```

# WWSP

```
scm> (if (or #t (/ 1 0)) 1 (/ 1 0))
```

```
scm> (if (> 4 3) (+ 1 2 3 4) (+ 3 4 (* 3 2)))
```

```
scm> ((if (< 4 3) + -) 4 100)
```

```
scm> (if 0 1 2)
```

# WWSP

```
scm> (if (or #t (/ 1 0)) 1 (/ 1 0))
```

```
1
```

```
scm> (if (> 4 3) (+ 1 2 3 4) (+ 3 4 (* 3 2)))
```

```
scm> ((if (< 4 3) + -) 4 100)
```

```
scm> (if 0 1 2)
```

# WWSP

```
scm> (if (or #t (/ 1 0)) 1 (/ 1 0))
```

```
1
```

```
scm> (if (> 4 3) (+ 1 2 3 4) (+ 3 4 (* 3 2)))
```

```
10
```

```
scm> ((if (< 4 3) + -) 4 100)
```

```
scm> (if 0 1 2)
```

# WWSP

```
scm> (if (or #t (/ 1 0)) 1 (/ 1 0))
```

```
1
```

```
scm> (if (> 4 3) (+ 1 2 3 4) (+ 3 4 (* 3 2)))
```

```
10
```

```
scm> ((if (< 4 3) + -) 4 100)
```

```
-96
```

```
scm> (if 0 1 2)
```

Can return symbols.

Evaluate the returned symbols  
to be procedures.

# WWSP

```
scm> (if (or #t (/ 1 0)) 1 (/ 1 0))
```

```
1
```

```
scm> (if (> 4 3) (+ 1 2 3 4) (+ 3 4 (* 3 2)))
```

```
10
```

```
scm> ((if (< 4 3) + -) 4 100)
```

```
-96
```

```
scm> (if 0 1 2)
```

```
1
```

# SPECIAL FORMS

## LAMBDAS & DEFINE

- All functions are secretly lambda expressions.
- When a lambda expression is called, a new frame is created.
- **(lambda (<parameters>) <expr>)**
- To call the lambda procedure:
- **((lambda (<parameters>) <expr>) <arguments>)**

# SPECIAL FORMS

## LAMBDAS & DEFINE

- **(define (<func name> <parameters>) <expr>)**
- Can be translated as.
- **(define <func name> (lambda (<parameters>) <expr>))**
- This is why procedure name is returned for **define**

# SPECIAL FORMS

## LAMBDAS & DEFINE

```
scm> (define x 3)
```

```
x
```

```
scm> (define y 4)
```

```
y
```

```
scm> ((lambda (x y) (+ x y)) 6 7)
```

```
13
```

# SPECIAL FORMS

## LAMBDAS & DEFINE

```
scm> (define x 3)
x
scm> (define y 4)
y
scm> ((lambda (x y) (+ x y)) 6 7)
13
```

6 and 7 are passed in as arguments and bound to x and y  
in the lambda's local frame

# SPECIAL FORMS

## LAMBDAS & DEFINE

```
scm> (define square (lambda (x) (* x x)))  
square  
scm> (square 4)  
16
```

Lambda functions also values.

# SPECIAL FORMS

## LET

```
(let ( (<symbol_1> <expr_1>)
```

...

```
    (<symbol_n> <expr_n>) )  
<body> )
```

- Let binds symbol to expressions locally and then evaluates the body.
- Useful if you want to reuse values multiple times.
- Make code more readable. (Composition)

# SPECIAL FORMS

## LET

```
(let ( (<symbol_1> <expr_1>)
```

```
  ...
```

```
    (<symbol_n> <expr_n>) )  
<body> )
```

```
( (lambda (<symbol_1> ... <symbol_n>) <BODY>)  
  <expr_n> ... <expr_n>)
```

# SPECIAL FORMS

## LET

```
(let ( (<symbol_1> <expr_1>)
```

```
  ...
```

```
    (<symbol_n> <expr_n>) )  
<body> )
```

```
(define (sin x)
```

```
  (if (< x 0.000001)
```

```
    x
```

```
    (let ( (recursive-step (sin (/ x 3))) )
```

```
      (- (* 3 recursive-step)
```

```
      (* 4 (expt recursive-step 3))))))
```

# SPECIAL FORM

## COND

```
(cond (<p_1> <e_1>)
      (<p_2> <e_2>)
      ...
      (<p_n> <e_n>)
      (else <else-expr>))
```

- Nested if statements are complicated and hard to read.
- The **cond** forms checks each predicate expression pair.
- If the predicate is true, we evaluate the corresponding expression. Otherwise we continue to check the next pair.
- The else expression is evaluated if no predicate is true.

# SPECIAL FORM

## BEGIN

- Begin is a special form that takes in subexpressions.
- It evaluates all subexpressions in order.
- The value of a begin form is the value from evaluating the last subexpressions.

```
scm> (begin (factorial 4) (square 5))
```

```
25
```

```
scm> (begin (/ 1 0) (factorial 4))
```

```
Error
```

# PAIRS & LISTS

- The only data structure in scheme is list.
- Caveat: They are linked lists!
- We call each “link” a pair with a first value and a rest value.

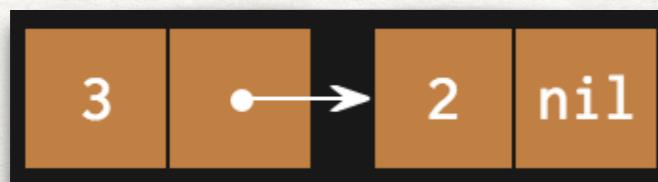
# PAIRS & LISTS

- Constructor:  $(\text{cons } 2 \text{ nil}) \rightarrow (2)$ 
  - nil is an empty list.
  - Obtain first element:  $(\text{car } (\text{cons } 2 \text{ nil})) \rightarrow 2$
  - Obtain second element:  $(\text{cdr } (\text{cons } 2 (\text{cons } 3 \text{ nil}))) \rightarrow (3)$
  - The second element is a list!



# PAIRS & LISTS

```
scm> nil  
()  
scm> (null? nil)  
#t  
scm> (cons 2 nil)  
(2)  
scm> (cons 3 (cons 2 nil))  
(3 2)
```



```
scm> (define a (cons 3 (cons 2 nil)))  
a  
scm> (car a)  
3  
scm> (cdr a)  
(2)  
scm> (car (cdr a))  
2  
scm> (define (len a)  
      (if (null? a)  
          0  
          (+ 1 (len (cdr a)))))  
len  
scm> (len a)  
2
```

# PAIRS & LISTS

- Well formed lists are those where the second element is nil or another linked list.

# PAIRS & LISTS

- Well formed lists are those where the second element is nil or another linked list.

```
scm> (cons 1 (cons 2 (cons 3 nil)))
```

```
(1 2 3)
```

```
scm> nil
```

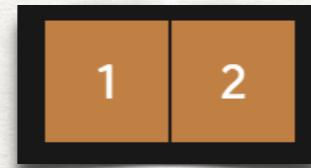
```
()
```



# PAIRS & LISTS

- Malformed list occurs when the second element is a value.
- A dot separates the first value and the second value.

```
scm> (cons 1 2)  
(1 . 2)
```



# PAIRS & LISTS

- Deep list occurs when the first element is another list!

```
scm> (define lst (cons 1 (cons (cons 2 (cons 3 nil)) (cons 4 (cons 5 nil)))))  
(1 (2 3) 4 5)
```

```
scm> (car lst)
```

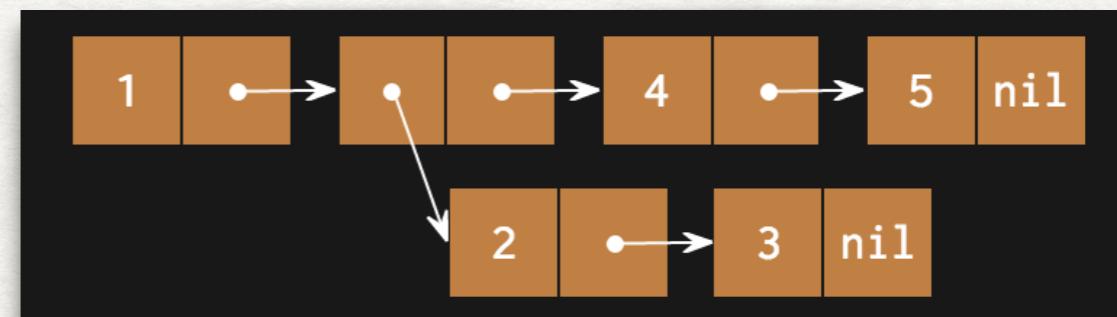
```
(2 3)
```

```
scm> (car (cdr (cdr lst)))
```

```
4
```

```
scm> (car (cdr (car (cdr lst))))
```

```
3
```



# PAIRS & LISTS

- We can also construct well-formed lists with the **list** operator.

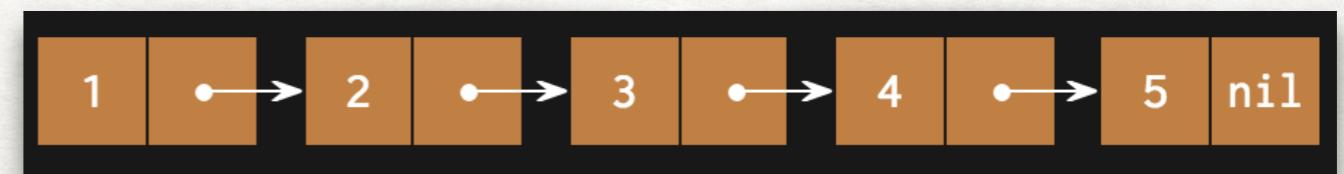
```
scm> (list 1 2 3 4 5)  
(1 2 3 4 5)
```



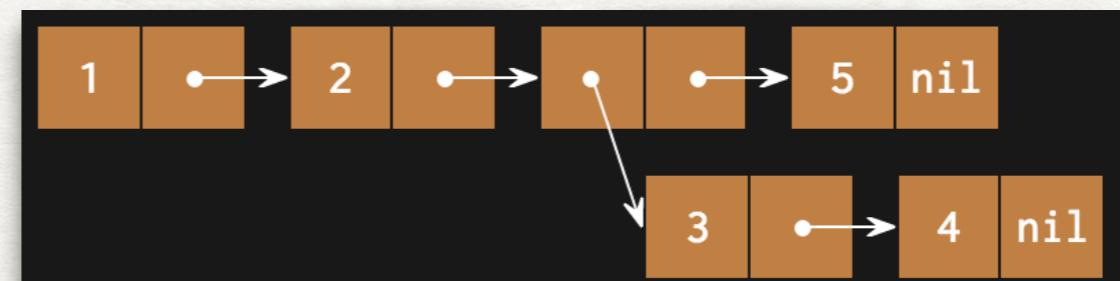
# PAIRS & LISTS

- We can also construct well-formed lists with the **list** operator.

```
scm> (list 1 2 3 4 5)  
(1 2 3 4 5)
```



```
scm> (list 1 2 (list 3 4) 5)  
(1 2 (3 4) 5)
```



List creates same # of pairs as the # of operands.  
Each operand will go into the first value of each pair.

# PAIRS & LISTS

- Or we can use quote form.

```
scm> '(1 2 3 4)
```

```
(1 2 3 4)
```

```
scm> '(3 . (2 1))
```

```
(3 2 1)
```

```
scm> '(define (foo x) x)
```

```
(define (foo x ) x)
```

```
scm> '(3 . (2 . (1 . nil)))
```

```
(3 2 1)
```

Note: open "(" and closing ")"  
parenthesis as **symbols** represent lists.

# PAIRS & LISTS

- Or we can use quote form.

```
scm> '(1 2 3 4)
```

```
(1 2 3 4)
```

```
scm> '(3 . (2 1))
```

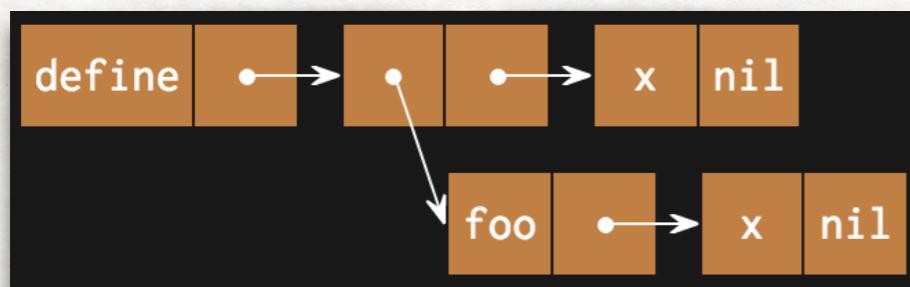
```
(1 2 3)
```

```
scm> '(define (foo x) x)
```

```
(define (foo x ) x)
```

```
scm> '(3 . (2 . (1 . nil)))
```

```
(3 2 1)
```



The quote form is propagated through the list.  
define and foo are symbols.

Note: open "(" and closing ")"  
parenthesis as symbols represent lists.

# PAIRS & LISTS

- Or we can use quote form.

```
scm> '(1 2 3 4)
```

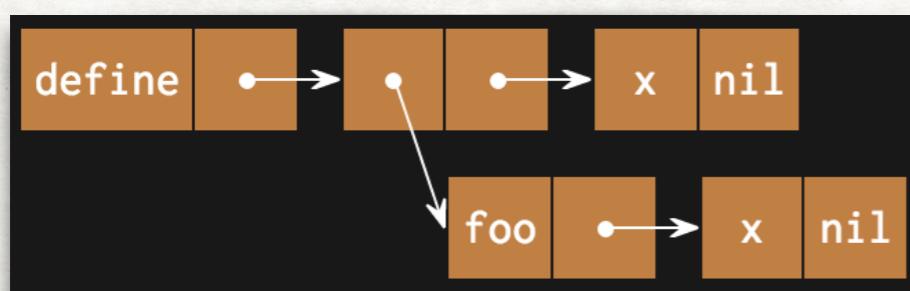
```
(1 2 3 4)
```

```
scm> '(3 . (2 1))
```

```
(1 2 3)
```

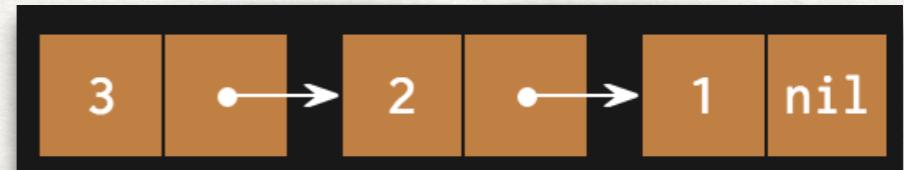
```
scm> '(define (foo x) x)
```

```
(define (foo x) x)
```



```
scm> '(3 . (2 . (1 . nil)))
```

```
(3 2 1)
```



The expression after the dot is the second element.

Since it is another list, the list is well-formed.

The quote form is propagated through the list.  
define and foo are symbols.

Note: open "(" and closing ")"  
parenthesis as symbols represent lists.

# HINTS

- Scheme has no iteration or objects. Only recursion and functions.
- For list code writing questions, it may seem easier to use iteration sometimes.
- We can turn recursion into iteration by defining a helper function that has an additional parameter **so-far**.
- This parameter is the list we have built thus far in our recursive calls.
- When we reach the base case, we can just return this **so-far** list.

# RECAP

- Scheme is a functional programming language.
- We can define variables and procedures with **define**
- Symbols have values that can be obtained if you evaluate the symbols.
- Scheme lists are linked lists.